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| 10-DIGIT PUID | Page 2 | /18 |
| RECITATION INSTRUCTOR | Page 3 | /28 |
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| RECITATION TIME | TOTAL | /100 |

DIRECTIONS

- 1. Write your name, 10-digit PUID, recitation instructor's name and recitation time in the space provided above. Also write your name at the top of pages 2, 3, and 4.
- 2. The test has four (4) pages, including this one.
- 3. Write your answers in the boxes provided.
- 4. You must show sufficient work to justify all answers unless otherwise stated in the problem. Correct answers with inconsistent work may not be given credit.
- 5. Credit for each problem is given in parentheses in the left hand margin.
- 6. No books, notes or calculators may be used on this test.
- (9) 1. Determine whether the following statements are true or false for any series $\sum_{n=1}^{\infty} a_n$. (Circle T or F. You do not need to show work).
 - (a) If $\lim_{n\to\infty} a_n$ does not exist, then $\sum_{n=1}^{\infty} a_n$ is divergent.

ТF

(b) If $0 \le a_n \le \frac{1}{n\sqrt{n}}$ for all n, then $\sum_{n=1}^{n-1} a_n$ is convergent.

TF

(c) If $\lim_{n\to\infty} \left|\frac{a_{n+1}}{a_n}\right| = 1$, then $\sum_{n=1}^{\infty} a_n$ is convergent.

TF

(12) 2. Determine whether each of the following series is convergent or divergent. (You do not need to show work).

(a)
$$\sum_{n=2}^{\infty} \frac{n+2}{n^2-1}$$

(b)
$$\sum_{n=1}^{\infty} \frac{5(-2)^{n+1}}{3^n}$$

.

$$(c) \sum_{n=1}^{\infty} \frac{5 - 2\sqrt{n}}{n^3}$$



(27) 3. Determine whether each series is convergent or divergent. You must verify that the conditions of the test are satisfied and write your conclusion in the small box.

(a)
$$\sum_{n=1}^{\infty} (-1)^{n-1} n e^{-\frac{n}{3}}$$

Show all necessary work here:

By the

test, the series is

(b) $\sum_{n=1}^{\infty} \frac{\sqrt{n^2+5}}{n^3+1}$

Show all necessary work here:

By the

test, the series is

(c)
$$\sum_{n=2}^{\infty} \frac{1}{n \ln n}$$

Show all necessary work here:

By the

test, the series is

(10) 4. Determine whether the series $\sum_{n=1}^{\infty} \frac{\cos(\frac{n}{2})}{n^2 + 4n}$ is absolutely convergent, conditionally convergent or divergent.

(9) 5. Consider the series $\sum_{n=1}^{\infty} \frac{(-1)^{n-1}}{4^n}$.

- (a) Write out the first five terms of the series.
- (b) Find the smallest number of terms that we need to add in order to estimate the sum of the series with error < 0.01.

- (16) 6. For the power series $\sum_{n=1}^{\infty} \frac{(-2)^n x^n}{\sqrt[4]{n}}$, find the following, showing all work.
 - (a) The radius of convergence R.

R =

(b) The interval of convergence. (Don't forget to check the end points).

Interval of convergence

(10) 7. Find the power series representation of $\frac{x}{1-2x}$ (about a=0) and give its interval of convergence

$$\frac{x}{1-2x} = \sum$$

Interval of convergence

(7) 8. Find the Taylor series for $f(x) = e^x$ centered at a = 3.

 $e^x = \sum$