NAME _ STUDENT ID _____ RECITATION INSTRUCTOR _____ RECITATION TIME _____

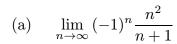
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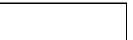
DIRECTIONS

- 1. Write your name, student ID number, recitation instructor's name and recitation time in the space provided above. Also write your name at the top of pages 2, 3, 4 and 5.
- 2. The test has five (5) pages, including this one.
- 3. Write your answers in the boxes provided.
- 4. You must show sufficient work to justify all answers. Correct answers with inconsistent work may not be given credit.
- 5. Credit for each problem is given in parentheses in the left hand margin.
- 6. No books, notes or calculators may be used on this test.
- 1. Circle the letter of the correct response. (You need not show work for this problem).
 - (a) Which of the following statements are true?
 - (I) If $\sum_{n=1}^{\infty} a_n$ converges absolutely, then $\sum_{n=1}^{\infty} a_n$ converges.
 - (II) If $0 < a_n$ for all $n \ge 1$ and $\lim_{n \to \infty} \frac{a_{n+1}}{a_n} = 2$, then $\sum_{n=1}^{\infty} a_n$ converges.
 - (III) If $0 < a_n \le b_n$ for all $n \ge 1$ and $\sum_{n=1}^{\infty} b_n$ converges, then $\sum_{n=1}^{\infty} a_n$ diverges.
 - C. II and III only I only B. I and II only D. III only
 - (b) Which of the following series converge? (I) $\sum_{n=2}^{\infty} \frac{1}{n\sqrt{n^2-1}}$

 - (II) $\frac{1}{\sqrt{2}} \frac{1}{\sqrt{3}} + \frac{1}{\sqrt{4}} \frac{1}{\sqrt{5}} + \dots$
 - (III) $\frac{1}{\sqrt{2}} + \frac{1}{\sqrt{3}} + \frac{1}{\sqrt{4}} + \frac{1}{\sqrt{5}} + \dots$
 - II only B. I only C. I and II only D. II and III only E. all

(9) 2. Find the limit if it exists, or write DNE if the limit does not exist. (You need not show work for this problem).





(b) $\lim_{n \to \infty} \frac{-n^2 + 2n - 1}{3 - 4n + 3n^2}$



(c) $\lim_{n \to \infty} \sqrt[n]{5n^2}$



(8) 3. Find the sum of the series, if it converges.

$$\sum_{n=1}^{\infty} 5\left(\frac{4}{7}\right)^n$$

(10) 4. Use the integral test to determine whether the series $\sum_{n=2}^{\infty} \frac{1}{n(\ln n)^2}$ is convergent or divergent. You must show all work.

The series is

(10) 5. Determine whether the series $\sum_{n=1}^{\infty} \frac{\sin n}{n^2+1}$ diverges, converges conditionally, or converges absolutely. You must show all work.

The series

(6) 6. Determine whether the series $\sum_{n=1}^{\infty} \frac{n+1}{n+2}$ converges or diverges. You must justify your answer.

The series

(20) 7. Determine whether each series is convergent or divergent. You <u>must</u> justify your conclusion with a mathematically correct reason. Write your conclusion in the small box

(a) $\sum_{n=0}^{\infty} \frac{e^n}{n!}$

Show all necessary work here:

By the

test, the series is

(b)
$$\sum_{n=1}^{\infty} \frac{1}{\sqrt{n^3 + 1}}$$

Show all necessary work here:

By the

test, the series is

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(15) 8. Find the interval of convergence of the power series $\sum_{n=1}^{\infty} \frac{2}{3^{n+1}n^2} x^n$. Don't forget to test for convergence at the end points of the interval. You must show all work.



(10) 9. Given that $e^{-x^2} = 1 - x^2 + \frac{x^4}{2!} - \frac{x^6}{3!} + \dots$, approximate the value of the integral $\int_0^{\frac{1}{10}} e^{-x^2} dx$ with error less than 10^{-5} , using the <u>smallest possible</u> number of terms of the series. (You may leave your answer as a sum of fractions).

 $\int_0^{\frac{1}{10}} e^{-x^2} dx \approx$