## MA162 — EXAM I — SPRING 2017 — February 2, 2017 TEST NUMBER 01

## **INSTRUCTIONS:**

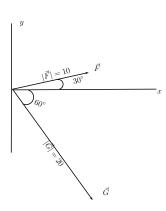
- 1. Do not open the exam booklet until you are instructed to do so.
- 2. Before you open the booklet fill in the information below and use a # 2 pencil to fill in the required information on the scantron.
- 3. MARK YOUR TEST NUMBER ON YOUR SCANTRON
- 4. Once you are allowed to open the exam, make sure you have a complete test. There are 7 different test pages (including this cover page).
- 5. Do any necessary work for each problem on the space provided or on the back of the pages of this test booklet. Circle your answers on this test booklet.
- 6. The exam has 11 problems and each one is worth 9 points; everyone gets 1 free point. The maximum possible score is 100 points. No partial credit.
- 7. Do not leave the exam room during the first 20 minutes of the exam.
- 8. If you do not finish your exam in the first 50 minutes, you must wait until the end of the exam period to leave the room.
- 9. After you have finished the exam, hand in your scantron and your test booklet to your recitation instructor.

## DON'T BE A CHEATER:

- 1. Do not give, seek or obtain any kind of help from anyone to answer questions on this exam. If you have doubts, consult only your instructor.
- 2. Do not look at the exam or scantron of another student.
- 3. Do not allow other students to look at your exam or your scantron.
- 4. You may not compare answers with anyone else or consult another student until after you have finished your exam, given it to your instructor and left the room.
- 5. Do not consult notes or books.
- 6. **Do not handle** phones or cameras, calculators or any electronic device until after you have finished your exam, given it to your instructor and left the room.
- 7. After time is called, the students have to put down all writing instruments and remain in their seats, while the TAs collect the scantrons and the exams.
- 8. Anyone who violates these instructions will have committed an act of academic dishonesty. Penalties for academic dishonesty include an F in the course. All cases of academic dishonesty will be reported to the Office of the Dean of Students.

I have read and understand the above statements regarding academic dishonesty:

STUDENT NAME:
STUDENT SIGNATURE:
STUDENT ID NUMBER:
SECTION NUMBER AND RECITATION INSTRUCTOR:



1. Let  $\vec{F}$  and  $\vec{G}$  be the two-dimensional vectors shown in the figure above. The tangent of the angle the vector  $\vec{F} + \vec{G}$  makes with the positive part of the x-axis is equal to

A. 
$$\frac{1+2\sqrt{3}}{2-\sqrt{3}}$$

B. 
$$\frac{1 - 2\sqrt{3}}{2 + \sqrt{3}}$$

C. 
$$\frac{1+5\sqrt{3}}{2+3\sqrt{3}}$$

D. 
$$\frac{1-5\sqrt{3}}{2-3\sqrt{3}}$$

E. 
$$\frac{1-4\sqrt{3}}{2+\sqrt{3}}$$

- 2. Find the center and the radius of the sphere  $4x^2 + 4y^2 + 4z^2 4x 12y + 8z = 2$ 
  - A. Center  $(\frac{1}{2}, -\frac{5}{4}, -1)$  and radius 2
  - B. Center  $(\frac{1}{2}, \frac{3}{4}, 1)$  and radius 2
  - C. Center  $(\frac{1}{2}, \frac{3}{4}, 1)$  and radius 4
  - D. Center  $(\frac{1}{2}, \frac{3}{2}, -1)$  and radius 2
  - E. Center  $(\frac{1}{2}, \frac{3}{2}, -1)$  and radius 4

- **3.** Find the number b such that the angle between the vectors  $\vec{u} = \vec{i} + \vec{j} + \vec{k}$  and  $\vec{v} = b\vec{i} \vec{j} + \vec{k}$  is equal to  $\frac{\pi}{3}$ .
  - A. b = 1
  - B.  $b = -\sqrt{6}$
  - C.  $b = \sqrt{2}$
  - D.  $b = \sqrt{6}$
  - E.  $b = -\sqrt{2}$

- 4. Which of the following statements are correct?
  - I) The vectors  $\vec{u} = 3\vec{i} + 2\vec{j} 2\vec{k}$  and  $\vec{v} = 2\vec{i} 2\vec{j} + \vec{k}$  are perpendicular.
  - II) The area of the parallelogram defined by  $\vec{a} = \vec{i} + 2\vec{j} + \sqrt{5} \ \vec{k}$  and  $\vec{i}$  is equal to 3.
  - III) The volume of the parallelepiped defined by  $\vec{a}=\vec{i}+\vec{j}+\vec{k},\ \vec{b}=2\vec{i}-\vec{j}$  and  $\vec{c}=-3\vec{i}+\vec{j}$  is equal to 1.
    - A. I and II only
    - B. I and III only
    - C. I, II and III
    - D. II and III only
    - E. III only

- **5.** Find the area enclosed by the curves  $x = 2y y^2$  and  $x = y^2$ 
  - A.  $\frac{1}{3}$
  - B.  $\frac{1}{2}$ C.  $\frac{2}{3}$

  - D. 1
  - E.  $\frac{5}{3}$

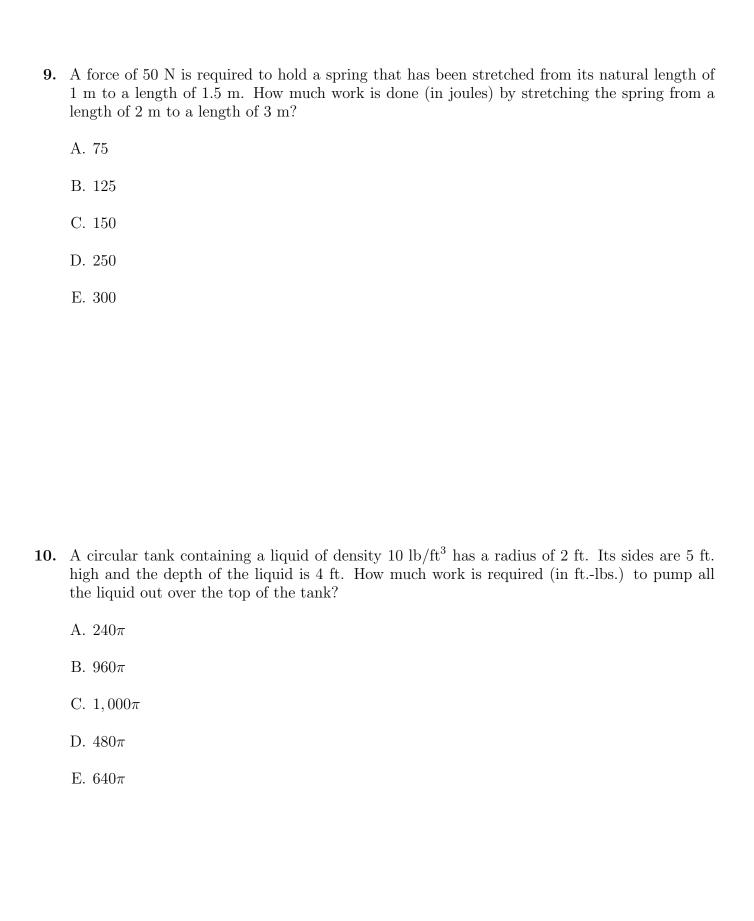
- **6.** Find the area of the region between the graph of  $y = x^2 4x + 3$ ,  $-1 \le x \le 1$ , and the x-axis.
  - A.  $\frac{11}{3}$
  - B.  $\frac{19}{3}$

  - C.  $\frac{20}{3}$ D.  $\frac{22}{3}$

- 7. Find the volume of the solid generated by revolving the region bounded by  $y = \sqrt{x}$ , x = 0 and y = 2 about the y-axis.
  - A.  $\frac{8}{3}\pi$
  - B.  $\frac{16}{5}\pi$
  - C.  $\frac{16}{3}\pi$
  - D.  $\frac{32}{5}\pi$
  - E.  $\frac{4}{5}\pi$

- 8. Use the method of cylindrical shells to find the volume generated by rotating the region bounded by the curves  $y = x x^2$  and y = 0, about the line x = -1.

  - A.  $\frac{\pi}{2}$ B.  $\frac{\pi}{3}$ C.  $\frac{2\pi}{3}$
  - D.  $\frac{\pi}{4}$
  - E.  $\frac{3\pi}{4}$



- 11. On a day in January, the temperature t hours after 8:00 am was  $T(t) = -10 + t^2$  degrees Fahrenheit. What was the average temperature between 8:00 am and 2:00 pm?
  - A. -4
  - B. 2
  - C. 4
  - D. 8
  - E. 12